

Course Title: **Compilers and Languages**
Date: 28.11.2015 (First term)Course Code: CCE3113 3rd year
Allowed time: 1 hrs and 30 minutes**Answer the following questions:****Question No. 1****(8 marks)****1. True or false? Are the following regular expressions exactly equivalent?**
(5 marks- 1 mark for each one)

- | | |
|-----------------------|-----------|
| a) $x?x^*$ | x^* |
| b) $y^* z^*$ | $(y z)^*$ |
| c) a^*b^* | $(ab)^*$ |
| d) $(P Q \epsilon)^*$ | $(P Q)^*$ |
| e) $(0 1)?$ | $0? 1?$ |

Answers: **True, False, False, True, True.****2. Explain why the grammar below is ambiguous.****(3 marks)** $S \rightarrow 0A \mid 1B$ $A \rightarrow 0AA \mid 1S \mid 1$ $B \rightarrow 1BB \mid 0S \mid 0$

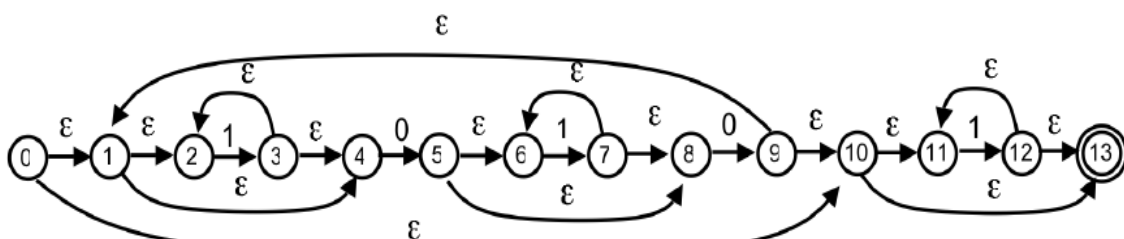
The grammar is ambiguous because we can find strings which have multiple derivations:

 $S \Rightarrow 0A \Rightarrow 00AA \Rightarrow 001S1 \Rightarrow 0011B1 \Rightarrow 001101$ $S \Rightarrow 0A \Rightarrow 00AA \Rightarrow 0011S \Rightarrow 00110A \Rightarrow 001101$ **Question No. 2****(6 marks)****1. Considering the alphabet $\Sigma = \{0,1\}$**

- Construct a Non-Deterministic-Finite Automaton (NFA) that is able to recognize the sentences generated by the regular expression $(1^*01^*0)^*1^*$.
- Convert the NFA to a DFA.
- Does the string $w = "1010"$ belong to the language generated by this regular expression? Justify.

Answer

(a) The NFA is as shown below



(b)

$S_0 = \epsilon\text{-closure}(0) = \{0, 1, 2, 4, 10, 11, 13\}$ – this is a final state because of 13

$S_2 = \epsilon\text{-closure}(S_0, 0) = \{5, 6, 8\}$

$S_1 = \epsilon\text{-closure}(S_0, 1) = \{2, 3, 4, 11, 12, 13\}$ – final state

$\epsilon\text{-closure}(S_1, 0) = \{5, 6, 8\} = S_2$

$\epsilon\text{-closure}(S_1, 1) = \{2, 3, 4, 11, 12, 13\} = S_1$

$\epsilon\text{-closure}(S_2, 0) = \{1, 2, 4, 9, 10, 11, 13\}$ – final state

$\epsilon\text{-closure}(S_2, 1) = \{6, 7, 8\}$

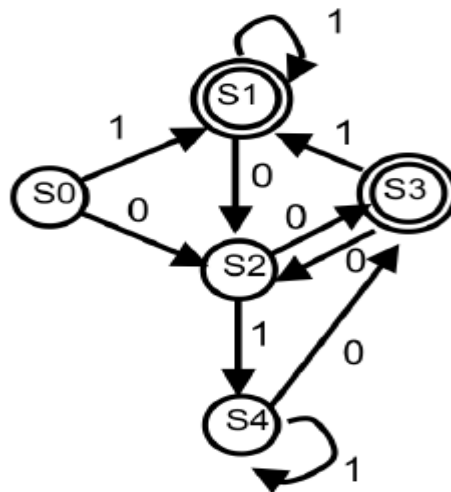
$\epsilon\text{-closure}(S_4, 0) = \{1, 2, 4, 9, 10, 11, 13\} = S_3$

$\epsilon\text{-closure}(S_4, 1) = \{6, 7, 8\} = S_4$

$\epsilon\text{-closure}(S_3, 0) = \{5, 6, 8\} = S_2$

$\epsilon\text{-closure}(S_3, 1) = \{2, 3, 4, 11, 12, 13\} = S_1$

This results in the DFA shown below with starting state S_0 .



(c) Yes, the string $w = "1010"$ belongs to the language generated by this regular expression

$S_0 \xrightarrow{1} S_1 \xrightarrow{0} S_2 \xrightarrow{1} S_4 \xrightarrow{0} S_3 \dots$ which is an accepting state

Question No. 3

(6 marks)

Given the following grammar G:

$S \rightarrow E$

$E \rightarrow T E'$

$E' \rightarrow + T E' \mid \epsilon$

$T \rightarrow F T'$

$T' \rightarrow * F T' \mid \epsilon$

$F \rightarrow (E) \mid d$

a) Find FIRST and FOLLOW of each non-terminal of the grammar.

N	FIRST(N)	FOLLOW(N)
S	(,d	{}
E	(,d), \$
E'	+), \$
T	(,d	+,), \$
T'	*	+,), \$
F	(, d	*, +,), \$

b) Construct the LL(1) parsing table for the grammar.

N \ Σ	d	+	*	()	\$
S	E\$	err	err	E\$	err	err
E	TE'	err	err	TE'	err	err
E'	err	+TE'	err	err	ϵ	ϵ
T	FT'	err	err	FT'	err	err
T'	err	ϵ	*FT'	err	ϵ	ϵ
F	F \rightarrow d	error	error	F \rightarrow (E)	error	error

c) Is this grammar LL(1) ? why?

Yes, since there is at most one rule in every cell of the LL(1) table.

Best wishes

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